

CROSS-INTERACTION CONSTANTS AS A MEASURE OF THE TRANSITION STATE STRUCTURE. PART 8. MECHANISM OF THE REACTION OF 2-PHENYLETHYL BENZENESULPHONATES WITH BENZYLAMINE IN ACETONITRILE

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The kinetics of reactions between 2-phenylethyl benzenesulphonates (2-PEB) and benzylamines in acetonitrile at 65.0 °C have been studied; the mechanism was examined on the basis of the sign and magnitude of cross-interaction constants ρ_{ij} and β_{ij} . In contrast to the reactions of 2-PEB with anilines in methanol, participation of the aryl-assisted pathway was negligible, with a strong indication that the reaction proceeds largely by an intermolecular S_Ni mechanism with a four-centre transition state (TS). The effect of substituents on the TS variation was in accord with the predictions of the quantum mechanical model.

INTRODUCTION

The nucleophilic displacement reactions of 2-phenylethyl compounds have attracted considerable attention in connection with the involvement of an aryl participation.¹ In such reactions there is a three-way competition in the rate-determining displacement of the leaving group by the solvent (k_s), nucleophiles other than the solvent (k_N) and neighbouring aryl groups (k_A), as shown in Scheme 1.¹

In previous work,¹ we reported the results of kinetic studies of the reactions between 2-phenylethyl benzenesulphonates (2-PEB) with anilines in methanol at 65.0 °C, showing that the overall reaction proceeded by a dissociative S_N2 mechanism with a relatively small degree of aryl participation and the possibility of four-centre transition state (TS) in an intermolecular S_Ni mechanism² for the aryl-unassisted pathway. These conclusions were based on the magnitude of the cross-interaction constants ρ_{ij} defined by³

$$\log(k_{ij}/k_{HH}) = \rho_i\sigma_i + \rho_j\sigma_j + \rho_{ij}\sigma_i\sigma_j \quad (1)$$

The magnitude of the cross-interaction constants reflect the strength of the indirect interaction between substituents i and j through reaction centres R_i and R_j when both substituents interact with their respective centres simultaneously in the TS (Scheme 2), and provides a useful measure of bond length, r_{ij} .³

It has been shown that r_{ij} is linearly related to $\log(|\rho_{ij}|^{-1})$:

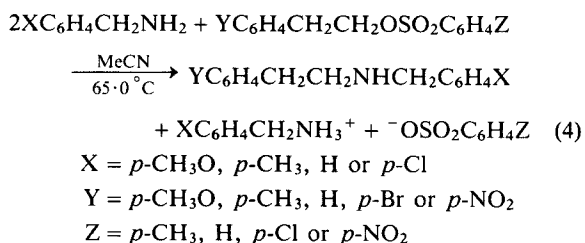
$$r_{ij} = \alpha + \beta \log(|\rho_{ij}|^{-1}) \quad (2)$$

where α and β are constants which depend on the rows of the Periodic Table for the two atoms being bonded at constant temperature.⁴ We have since introduced the Brønsted type of cross-interaction constant β_{ij} :

$$\log(k_{ij}/k_{HH}) = \beta_i\Delta pK_i + \beta_j\Delta pK_j + \beta_{ij}\Delta pK_i\Delta pK_j \quad (3)$$

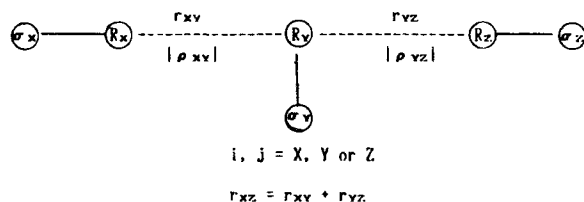
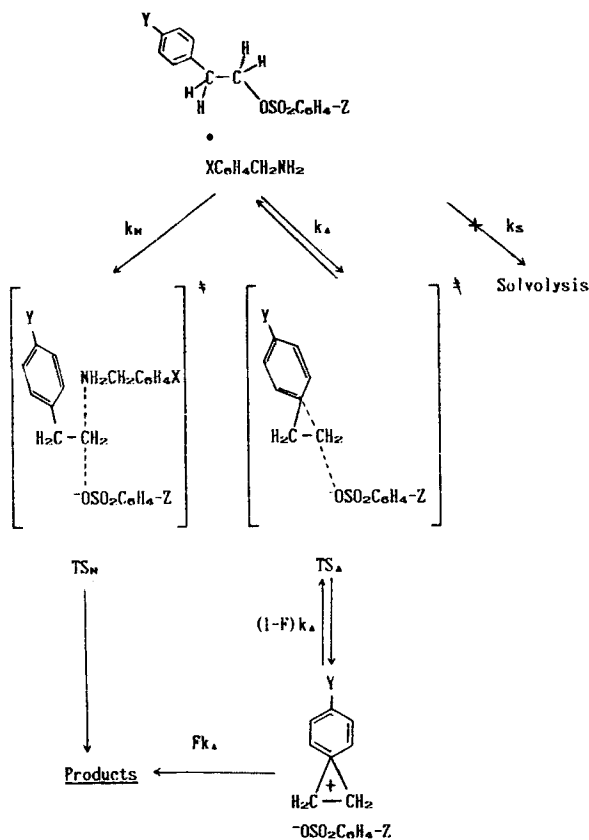
and applied them to the rationalization of mechanistic details involved in a variety of reactions.

In this paper, we report the results of kinetic studies of the reactions between 2-PEB and benzylamines (BA) in acetonitrile at 65.0 °C, equation (4), elaborating on the mechanism based on various cross-interaction constants ρ_{ij} and β_{ij} determined from k_{ij} values by multiple linear regressions using equations (1) and (3).



RESULTS AND DISCUSSION

Second-order rate constants, k_2 , for the reaction of 2-PEB with benzylamines [equation (4)] were obtained from slopes of pseudo-first-order rate constants, k_1^{obs} ,



versus benzylamine concentration, [BA] [equation (5), Table 1].

$$k_1^{\text{obs}} = k_1 + k_2[\text{BA}] \quad (5)$$

Solvolysis of 2-PEB in acetonitrile⁵ can be safely ruled out from zero intercepts, $k_1 \approx 0$, in equation (5) in all cases. The magnitudes of k_2 are approximately twice those for the corresponding reactions of 2-PEB with anilines in methanol at the same temperature.¹ The rate increases with a more electron-withdrawing substituent in the leaving group ($Z = \text{EWS}$) and with a more

Table 1. Second-order rate constants ($k_2 \times 10^4 \text{ l mol}^{-1} \text{ s}^{-1}$) for the reactions between $\text{YC}_6\text{H}_4\text{CH}_2\text{CH}_2\text{OSO}_2\text{C}_6\text{H}_4\text{Z}$ and $\text{XC}_6\text{H}_4\text{CH}_2\text{NH}_2$ in acetonitrile at 65.0°C

Z	X	Y				
		<i>p</i> -CH ₃ O	<i>p</i> -CH ₃	H	<i>p</i> -Br	<i>p</i> -NO ₂
<i>p</i> -NO ₂	<i>p</i> -CH ₃ O	55.3	56.2	56.9	56.5	56.2
	<i>p</i> -CH ₃	48.3	48.9	51.0	50.2	50.4
	H	36.9	38.2	39.0	37.9	37.4
	<i>p</i> -Cl	25.9	26.9	27.5	26.1	25.9
<i>p</i> -Cl	<i>p</i> -CH ₃ O	12.3	12.6	12.8	12.8	12.1
	<i>p</i> -CH ₃	10.7	10.8	11.1	10.8	10.2
	H	8.39	8.45	8.69	8.39	8.13
	<i>p</i> -Cl	6.02	6.10	6.25	6.17	5.83
H	<i>p</i> -CH ₃ O	6.46	6.53	6.61	6.64	6.17
	<i>p</i> -CH ₃	5.69	5.79	6.03	5.97	5.43
	H	4.47	4.57	4.75	4.51	4.27
	<i>p</i> -Cl	3.31	3.37	3.47	3.51	3.24
<i>p</i> -CH ₃	<i>p</i> -CH ₃ O	3.89	3.89	4.01	3.98	3.80
	<i>p</i> -CH ₃	3.47	3.48	3.63	3.63	3.47
	H	2.84	2.88	2.98	2.91	2.69
	<i>p</i> -Cl	2.11	2.16	2.24	2.19	2.04

electron-dominating substituent in the nucleophile ($X = \text{EDS}$).

The rate is almost insensitive, however, to substituent changes in the substrate (Y). A slight decrease in rate ($< 7\%$) is observed with both $Y = \text{EWS}$ and $Y = \text{EDS}$. This is in contrast with a slight increase in rate induced by $Y = \text{CH}_3\text{O}$ in the reaction of 2-PEB with anilines in methanol¹ and the relatively strong rate enhancement in solvolysis in ethanol acetic acid and formic acid.⁶ Since the *p*-CH₃O substituent is considered to be a strong phenyl group activator for the aryl-assisted process, k_A ,⁶ such an insensitivity of substituents (Y) in the substrate indicate that the aryl-assisted pathway is less important in the nucleophilic substitution reaction (4) than in solvolysis. This may be especially true when the rate of the nucleophilic pathway, k_N , is fast enough that the competition of the aryl-assisted path becomes negligible.¹

Variations of Hammett ρ_X and Brønsted β_X (β_N) parameters (obtained by varying substituent X in the nucleophile) with substituents Y in the substrate and Z in the leaving group (LG) are summarized in Table 2.

The ρ_X values are negative and approximately half those for the reaction with aniline¹ owing to an intervening CH₂ group in benzylamine.⁷ The magnitudes of ρ_X and β_X increase with a better LG ($Z = \text{p-NO}_2$), but vary very little with the substituent in the substrate (Y). It is barely observable that both $Y = \text{EWS}$ and $Y = \text{EDS}$ tend to have slightly greater $|\rho_X|$ and $|\beta_X|$.

The ρ_Z and β_Z (β_{LG}) values (obtained by varying substituent Z in the LG) are shown in Table 3. The magnitudes of ρ_Z and β_Z increase with a more EDS in the nucleophile ($X = \text{p-CH}_3$) and again vary very little with the substituent Y in the substrate. β_X is greater

Table 2. Hammett ρ_X^a and Brønsted β_X^a values for reaction (4)^b

Z	Parameter	Y				
		<i>p</i> -CH ₃ O	<i>p</i> -CH ₃	H	<i>p</i> -Br	<i>p</i> -NO ₂
<i>p</i> -NO ₂	ρ_X	-0.67	-0.65	-0.65	-0.69	-0.69
	β_X	0.67	0.65	0.67	0.71	0.72
<i>p</i> -Cl	ρ_X	-0.63	-0.63	-0.63	-0.64	-0.63
	β_X	0.62	0.62	0.62	0.61	0.61
H	ρ_X	-0.59	-0.58	-0.58	-0.57	-0.57
	β_X	0.59	0.59	0.60	0.57	0.56
<i>p</i> -CH ₃	ρ_X	-0.54	-0.51	-0.51	-0.53	-0.56
	β_X	0.54	0.52	0.52	0.55	0.57

^a Correlation coefficients are better than 0.998 at the 99% confidence level in all cases.

^b The pK_a values of BA were taken from Ref. 13.

Table 3. Hammett ρ_Z^a and Brønsted β_Z^a values for reaction (4)^b

X	Parameter	Y				
		<i>p</i> -CH ₃ O	<i>p</i> -CH ₃	H	<i>p</i> -Br	<i>p</i> -NO ₂
<i>p</i> -CH ₃ O	ρ_Z	1.21	1.22	1.21	1.21	1.21
	β_Z	-0.40	-0.41	-0.40	-0.40	-0.41
<i>p</i> -CH ₃	ρ_Z	1.20	1.20	1.20	1.20	1.23
	β_Z	-0.40	-0.40	-0.40	-0.40	-0.41
H	ρ_Z	1.18	1.18	1.18	1.18	1.21
	β_Z	-0.39	-0.40	-0.39	-0.39	-0.40
<i>p</i> -Cl	ρ_Z	1.15	1.16	1.15	1.13	1.16
	β_Z	-0.38	-0.39	-0.38	-0.38	-0.39

^a Correlation coefficients are better than 0.998 at the 99% confidence level in all cases.

^b The pK_a values were taken from Ref. 14.

than β_Z , suggesting a greater degree of bond formation than bond breaking in the TS.

In this reaction, a stronger nucleophile ($\sigma_X < 0$) and/or nucleofuge ($\sigma_Z > 0$) lends to a greater degree of bond breaking ($\Delta r_{YZ} > 0$) and/or formation ($\Delta r_{XY} < 0$), resulting in a 'late' TS conforming to the predictions by the quantum mechanical (QM) model.^{3g,8} This means that reaction (4) constitutes an intrinsically controlled series following the relationships

$$\begin{aligned}\Delta r_{XY} &= \lambda \sigma_Z \\ \Delta r_{YZ} &= \lambda' \sigma_X \\ \lambda < 0 \text{ and } \lambda' < 0\end{aligned}\quad (6)$$

where λ and λ' are negative constants.^{1,3g,i,p,9}

The ρ_Y values for reaction (4) are summarized in Table 4. Their sign is mostly negative, indicating a slightly greater degree of bond breaking than of bond formation, in contrast to the conclusion above based on

Table 4. Hammett ρ_Y values for reaction (4)^a

Z	X			
	<i>p</i> -CH ₃ O	<i>p</i> -CH ₃	H	<i>p</i> -Cl
<i>p</i> -NO ₂	0.00	0.01	0.00	-0.01
<i>p</i> -Cl	-0.01	-0.02	-0.02	-0.02
H	-0.02	-0.02	-0.03	-0.01
<i>p</i> -CH ₃	-0.01	0.00	-0.03	-0.02

^a The linearities of the plots were unsatisfactory in most cases since there were tendencies to form two branches by EWS and EDS. The values are therefore only approximate guides.

the magnitudes of ρ_X and β_Z . However, the magnitude is very small indeed, as we expected from the insensitivity of ρ_X and ρ_Z with the substituent Y in the substrate. One reason for this negligible $|\rho_Y|$ is the fall-off of the substituent effect susceptibility by a factor of 2.4–2.8 owing to an intervening CH₂ group (β -CH₂) in the substrate,⁷ and another may well be a near charge balance owing to approximately the same degree of bond formation and breaking. These two factors immediately rule out any significant participation of the aryl group (k_A) in the rate-determining step, since the aryl-assisted pathway has the TS structure which is not consistent with the two factors; the aryl-assisted intermediate has no CH₂ group corresponding to β -CH₂ with a unit positive charge.

The k_2 values in Table 1 were subjected to a multiple linear regression analysis¹¹ using equations (1) and (3), and cross-interaction constants ρ_{XY} , ρ_{YZ} , ρ_{XZ} and β_{XZ} were determined.³ The results are summarized in Table 5. The signs of these parameters are consistent with those expected from the predictions of TS variation by the QM model.⁸ The very small magnitudes of ρ_{XY} and ρ_{YZ} are again partly due to the intervening CH₂ groups in the nucleophile, BA, and substrate, 2-PEB.⁷ Since the fall-off factor for one CH₂ group is in the range 2.4–2.8, $|\rho_{XY}|$ should decrease by a factor of (2.4–2.8)² in comparison with those for the reactions of anilines with 1-phenylethyl (1-PEB), ($|\rho_{XY}| \approx 0.21$)^{3h,i} or the benzyl series ($|\rho_{XY}| \approx 0.70$).³ⁱ Rough estimates give 0.03 for 1-PEB and 0.10 for the benzyl series when the fall-off of (2.6)² is applied, showing that the degree of bond formation is small, being approximately the same as that of the 1-PEB series.^{3h} However $|\rho_{YZ}|$ is smaller than that for the reaction of 1-PEB^{3h} when the fall-off factor is allowed for. Since the reaction conditions, i.e. solvent and temperature, are different,³ these comparisons are only approximate.

The magnitudes of ρ_{XZ} and β_{XZ} are strikingly large, however; again, if we apply the fall-off factor to $|\rho_{XZ}|$, the magnitude amplifies to nearly that for the reaction of aniline and 1-PEB ($|\rho_{XZ}| \approx 0.50$).^{3h,i} Since we are free from the fall-off factors in the Brønsted-type coefficients, β_{XZ} values can be directly compared.³ⁿ Some examples of β_{XZ} values are given in Table 6.

Table 5. Hammett and Brønsted (in parentheses)^a type cross-interaction constants for reaction (4)

Z	ρ_{XY}	Correlation coefficient	X	ρ_{YZ}	Correlation coefficient	Y	ρ_{XZ}	Correlation coefficient
<i>p</i> -NO ₂	-0.04	0.997	<i>p</i> -CH ₃ O	0.02	0.999	<i>p</i> -CH ₃ O	-0.13 (-0.22)	1.000 (0.992)
<i>p</i> -Cl	-0.01	0.997	<i>p</i> -CH ₃	0.02	0.999	<i>p</i> -CH ₃	-0.12 (-0.19)	1.000 (0.992)
H	-0.02	0.994	H	0.03	1.000	H	-0.13 (-0.21)	1.000 (0.992)
<i>p</i> -CH ₃	-0.03	0.994	<i>p</i> -Cl	0.01	0.999	<i>p</i> -Br	-0.16 (-0.29)	0.999 (0.992)
						<i>p</i> -NO ₂	-0.15 (-0.30)	1.000 (0.993)

^a The pK_a values of sulphonic acids were taken from Ref. 15 and the pK_a values for BA from Ref. 13.

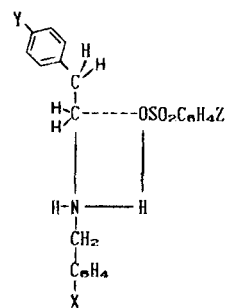
Table 6. Comparison of Brønsted type cross-interaction constants

Reaction	Reactants		β_{XZ}	Correlation coefficient	Ref.
A	XC ₆ H ₄ NH ₂ + YC ₆ H ₄ COCH ₂ OSO ₂ C ₆ H ₄ Z	MeOH 40.0 °C	0.19	0.995	3g
B	XC ₆ H ₄ CH ₂ NH ₂ + YC ₆ H ₄ COCH ₂ OSO ₂ C ₆ H ₄ Z	MeOH 45.0 °C	0.17	0.995	3m
C	XC ₆ H ₄ NH ₂ + YC ₆ H ₄ CH ₂ OSO ₂ C ₆ H ₄ Z	MeOH 35.0 °C	-0.06	0.996	3a
D	XC ₆ H ₄ N(CH ₃) ₂ + YC ₆ H ₄ CH(CH ₃)OSO ₂ C ₆ H ₄ Z	MeOH 35.0 °C	-0.11	0.989	3l
E	XC ₆ H ₄ NH ₂ + YC ₆ H ₄ CH(CH ₃)OSO ₂ C ₆ H ₄ Z	MeOH 25.0 °C	-0.32	0.987	3h
F	XC ₆ H ₄ NH ₂ + YC ₆ H ₄ CH ₂ CH ₂ OSO ₂ C ₆ H ₄ Z	MeOH 65.0 °C	-0.28	0.995	1
G	XC ₆ H ₄ CH ₂ NH ₂ + YC ₆ H ₄ CH ₂ CH ₂ OSO ₂ C ₆ H ₄ Z	MeOH 65.0 °C	-0.21	0.992	This work

The sign and magnitude of β_{XZ} for reaction (4), i.e. G, are nearer to those of reactions E and F but much greater than those of reactions C and D. This unusually large $|\rho_{XZ}|$ (corrected for the fall-off factor) and $|\beta_{XZ}|$ are indeed an indication that reaction (4) also proceeds largely by an intermolecular S_Ni mechanism with a four-centre TS, (Scheme 3), as we concluded for reactions E and F in previous papers;^{1,3h} the magnitude of cross-interaction is inversely proportional to the distances between reaction centres (Scheme 2), equation (2),⁴ so that $|\rho_{XZ}|$ should be the smallest instead of the greatest found since r_{XZ} ($=r_{XY} + r_{YZ}$) is greater than either r_{XY} or r_{YZ} .^{3h}

Hence of the three reaction paths conceivable for reaction (4), direct displacement, k_N , aryl-assisted, k_Δ , and intermolecular, S_Ni , the last mechanism with a four-centre TS is the most likely based on the sign and magnitude of the cross-interaction constants. In this

mechanism the nucleophile is required to approach from the front, forming a by-pass hydrogen bridge, which greatly enhances the interaction between the substituent in the nucleophile (X) and in the LG (Z).^{3c,h}



Scheme 3

EXPERIMENTAL

Materials. Benzylamines^{3i,p} and acetonitrile^{3p} were used after appropriate purification as described previously. 2-Phenylethyl benzenesulphonates were prepared and purified as described.¹

Rate constants. Rates were measured conductimetrically¹ at 65.0°C in acetonitrile. Pseudo-first-order rate constants, k_1^{obs} , were determined by the Guggenheim method¹⁰ with a large excess of benzylamine; [2-PEB] $\approx 10^{-3}$ M and [BA] ≈ 0.06 – 0.15 M. Second-order rate constants, k_2 were obtained from the slope of equation (5). The absence of solvolysis⁵ in acetonitrile was confirmed by zero intercepts, $k_1 = 0$ in equation (5), in all cases. No elimination products of 2-PEB were found in the preliminary tests. These are also evident from the large values of $|\rho_{\text{xz}}|$ since if there were any of these complications, the magnitude of ρ_{xz} would be small.

The linearity of the plot [equation (5)] was good, with correlation coefficients of better than 0.998 with a 99% confidence limit¹² (more than four [BA] values were used). The k_2 values listed in Table 1 are averages obtained by more than two runs, and were reproducible to within $\pm 5\%$.

Product analysis. Products of the reagent of 2-PEB with BA ($\text{PhCH}_2\text{CH}_2\text{NHCH}_2\text{Ph}$ and $\text{PhCH}_2\text{NH}_3^+ \text{SO}_3\text{PhCH}_3$) were identified by thin-layer chromatography, IR and NMR spectrometry and elemental analysis.

N-(2-Phenylethyl)benzylamine showed ν_{max} 3400 (secondary aromatic amine) and 1360 cm^{-1} (CN of secondary aromatic NH); δ 7.3 (Ph, 10H, m), 3.7 (α -CH₂, 4H, s), 2.8 (β -CH₂, 2H, s) and 1.9 (NH, 1H, s). $R_F = 0.55$ [developing solvent, cyclohexane–ethyl acetate (5:1)]. Found: C, 85.14; H, 8.19; N, 6.55. $\text{C}_{14}\text{H}_{17}\text{NO}_3\text{S}$ requires C, 85.26; H, 8.11; N, 6.63%.

Benzylammonium toluene-*p*-sulphonate was insoluble in organic solvents and had m.p. 198–200°C; ν_{max} 3400, 2600, 1600 and 1495 (NH_3^+) and 1210, 1170, 565 and 490 cm^{-1} (SO_3^-); δ 7.5 (Ph, 9H, m), 4.2 (CH₂, 2H, s), 3.1 (NH_3^+ , 3H, s) and 2.4 (CH₃, 3H, s). Found: C, 60.05; H, 6.21; N, 5.16. $\text{C}_{14}\text{H}_{17}\text{NO}_3\text{S}$ requires C, 60.19; H, 6.13; N, 5.01%.

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